SHED: Shannon Entropy Descriptors from Topological Feature Distributions

Elisabet Gregori-Puigjané and Jordi Mestres*
Chemogenomics Laboratory, Research Unit on Biomedical Informatics, Institut Municipal d’Investigació Médica and Universitat Pompeu Fabra, Passeig Marítim de la Barceloneta 37-49, 08003 Barcelona, Catalonia, Spain

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A novel set of molecular descriptors called SHED (SHannon Entropy Descriptors) is presented. They are derived from distributions of atom-centered feature pairs extracted directly from the topology of molecules. The value of a SHED is then obtained by applying the information-theoretical concept of Shannon entropy to quantify the variability in a feature-pair distribution. The collection of SHED values reflecting the overall distribution of pharmacophoric features in a molecule constitutes its SHED profile. Similarity between pairs of molecules is then assessed by calculating the Euclidean distance of their SHED profiles. Under the assumption that molecules having similar pharmacological profiles should contain similar features distributed in a similar manner, examples are given to show the ability of SHED for scaffold hopping in virtual chemical screening and pharmacological profiling compared to that of substructural BCI fingerprints and three-dimensional GRIND descriptors.

INTRODUCTION

The generation of mathematical representations for molecules has long been an active line of research in computational drug discovery. As a result, a large number and variety of molecular descriptors reflecting the one-dimensional, two-dimensional, and three-dimensional features of chemical structures have been devised.1 Once formulated, the relevance of these descriptors is often established according to their ability to reflect the pharmacological properties of molecules.2 Their potential impact in drug discovery is ultimately assessed when used, for example, in deriving quantitative structure—activity relationships from sets of molecules for which biological data is experimentally available3 or in performing similarity searches of large chemical libraries against a panel of reference active compounds.4

Within this context, atom-centered feature pairs constitute an attractive family of molecular descriptors.5 In their various formulations, they have been proven to show a decent performance on a diverse range of computational aspects in drug discovery covering quantitative structure—activity relationships,5 compound selection,6 virtual chemical screening,7–9 and virtual pharmacological profiling.10 In all of these studies, the actual computational encoding of the atom-centered feature-pair descriptors attempts to capture their overall distribution within a molecule by storing the occurrence of feature pairs at different distance ranges, either at the topological5–8 or geometrical level,9–11 to form a so-called binned fingerprint representation of each molecule. These molecular fingerprints are then used to assess the degree of resemblance between molecules according to different similarity metrics.12–14

Two aspects are worth emphasizing to understand the scope and limitations of this family of descriptors. On one hand, formulations based on geometric atom pair descriptors require three-dimensional coordinates and, thus, provide representations which are dependent on the conformation of the molecules.9–11 Consequently, this involves a 2D to 3D conversion of atomic coordinates and potentially the generation of multiple conformers for each molecule. On the other hand, formulations based on topological atom pair descriptors do not need three-dimensional coordinates and do not have this conformational dependency.5–8 However, they result in crisp representations of molecules that may not capture some of the essential information present only when using three-dimensional coordinates. A formulation based on a fuzzy description of topological features could be a good balance between the two approaches.

It is along these lines that a novel set of molecular descriptors is introduced. This new formulation takes advantage of the information-theoretical concept of Shannon entropy,15 an approach that is increasingly being applied to process chemical information.16–19 Accordingly, these new descriptors will be referred to as SHED, for SHannon Entropy Descriptors, and represent a means to quantify the variability displayed by topological distributions of atom-centered feature pairs in molecules. The following sections describe, first, the methodological details for obtaining SHED and, second, several application examples to assess their potential ability for scaffold hopping in virtual chemical screening and pharmacological profiling.

METHODS

The process of obtaining SHED from a chemical structure is illustrated in Figure 1 for dimetindene, a histamine H1 antagonist. The original input structure should be in MDL’s SD file format.20 From an SD file, each atom in a molecule is first mapped to a Sybyl atom type.21 Subsequently, each atom type is assigned currently to one or more of four atom-centered features, namely, hydrophobic (H), aromatic (R),

* Corresponding author e-mail: jmestres@imim.es.
acceptor (A), and donor (D). For example, an aliphatic C.3 carbon will be assigned to a hydrophobic feature (H), whereas a protonated N.4h nitrogen will be assigned to both aromatic and donor features (RD). Then, the shortest path length between atom-centered feature pairs is derived and its occurrence at different path lengths stored to create a feature-pair distribution. A maximum path length of 20 bonds was used. Feature pairs at distances over 20 bonds are accumulated in the last bin. As an example, the distribution of RD feature pairs within dimetindene is displayed. An equivalent distribution is derived for each of the 10 possible feature pairs resulting from all pair combinations of the four features used.

At this stage, the concept of Shannon entropy\(^1\) is applied to determine the variability of feature-pair distributions. Within this approach, the entropy, \(S\), of a population, \(P\), distributed in a certain number of bins (representing in this case the different path lengths), \(N \geq 20\), is given by

\[
S = - \sum_{i=1}^{N} \rho_i \ln \rho_i, \quad \rho_i = p_i/P
\]

where \(\rho_i\) and \(p_i\) are, respectively, the probability and the population at each bin \(i\) of the distribution. The values of \(S\) range between 0, reflecting the situation of the entire population being concentrated in a single bin, and a maximum number, \(S_{\text{max}} = \ln N\), reflecting the situation of a uniformly distributed population among all bins. In the case of dimetindene (Figure 1), RD pairs can be found at path lengths occupying seven bins and the variability in their occurrence at different path lengths stored to create a feature-pair distribution. A maximum path length of 20 bonds would be

\[
S_{\text{max}} = \ln 20 = 3.00 \ln 2 = 6.1074
\]

reflecting the situation of full uniform occupancy on seven bins. This \(E\) value will ultimately be the SHED for the RD feature pair. The set of SHED values obtained for the 10 possible feature pairs constitute the SHED profile of a molecule. As illustrated in Figure 1, SHED profiles are represented using a wheel chart, the circle in the chart indicating the \(E\) value (SHED) for the RD feature pair in dimetindene.

RESULTS AND DISCUSSION

The basic assumption is that molecules having similar features arranged in a similar way should display similar SHED profiles. The underlying question is to what extent SHED profiles derived from topology-based atom-centered feature-pair distributions of molecules are well-suited to recognize the presence of similar features arranged in a similar way around significantly different molecular scaffolds, an ability usually referred to as “scaffold hopping”\(^7\). To investigate this issue, an analysis of SHED profiles for molecules directed to different targets is presented next, followed by application examples on the use of SHED profiles for virtual chemical screening and pharmacological profiling.

Scaffold Hopping. Three diverse sets of molecules containing comparable features arranged similarly around essentially different scaffolds were selected. The structures of the molecules and their corresponding SHED profiles are collected in Figure 2. The first set includes a list of five known cyclooxygenase-1 inhibitors (COX-1: EC 1.14.99.1), namely, indomethacin (1), sulindac (2), fenbufen (3), ketoprofen (4), and indoprofen (5); the second set is a selection of five known thrombin inhibitors (Factor IIa: EC 3.4.21.5), namely, BM14.1224 (6), BM51.1047 (7), DAPA (8), 4-TAPAP (9), and 3-TAPAP (10); and the third set contains five estrogen receptor subtype \(\alpha\) antagonists (ER\(\alpha\): NR 3.A.1), namely, raloxifene (11), bazedoxifene (12), a tetrahydroisoquinoline ligand (13), LY326315 (14), and EM343 (15). As can be observed, despite the significant scaffold

Figure 1. Generation of a SHED profile from chemical structure.
diversity present in the three families of chemical structures, reasonably equivalent SHED profiles are obtained within each set. At the same time, the various target-directed SHED profiles are found to be essentially different from one another. Altogether, these results provide evidence of the potential applicability of SHED for identifying molecules containing similar features distributed similarly around diverse molecular scaffolds.

A characteristic worth emphasizing is the fact that size appears to be implicitly accounted for in the SHED profile of molecules, particularly in the SHED values corresponding to feature pairs involving hydrophobic and aromatic centers. For example, average values and standard deviations of SHED for the HH pairs found in COX-1 inhibitors, thrombin inhibitors, and ERα antagonists are, respectively, 4.40 ± 0.27, 5.95 ± 0.61, and 7.01 ± 0.17, which are indicative of the increasing size of compounds associated with those targets. In general, as compounds become bigger and more complex (in terms of combinations of features), the area filled by their SHED profiles would tend to be larger as well.

To assess quantitatively the degree of discrimination obtained when comparing different types of molecules, average Euclidean distances and standard deviations derived from the SHED profiles of the three sets of ligands are presented in Figure 3. The clear separation obtained between comparisons of pharmacophorically similar molecules and comparisons of molecules having essentially different feature distributions is remarkable. For example, average intraset
distances and standard deviations between COX-1, thrombin, and estrogen ligands are 1.17 ± 0.46, 2.23 ± 0.75, and 1.62 ± 0.71, respectively. In contrast, average interset distances and standard deviations when comparing COX-1/thrombin, COX-1/estrogen, and thrombin/estrogen ligands are 9.65 ± 0.92, 11.21 ± 0.70, and 4.35 ± 0.78, respectively. To put these results into perspective, the same exercise was done using BCI fingerprints, a representative 2D substructural fingerprint-based method widely used in compound clustering and similarity searching. In this case, the discrimination between intraset and interset comparisons is not as clear as that with SHED profiles, and a more fuzzy (less separation between intraset and interset distances) and less compact (larger values for standard deviations) picture appears. This outcome emphasizes the potential use of SHED in virtual screening applications.

Despite the attractive resemblance observed in the target-directed SHED profiles, both qualitatively in Figure 2 and quantitatively in Figure 3, those compounds represent only a focused subset extracted from the ample diversity of active compounds that could be identified and generated for a given target. In fact, having similar SHED profiles may well be a reflection of making analogous interactions within similar pockets in their respective targets. In reality, depending largely on the size of the protein binding cavity, its flexibility, and its degree of exposure to the solvent, ligands will bind to different pockets, exploit different interactions, and have a variety of solvent-exposed functional groups. In this scenario, a less compact picture will certainly emerge when visualizing the corresponding SHED profiles, but each SHED profile will be representative of a particular distribution of features allowed in an active compound for a given target.

Virtual Chemical Screening. Computational drug discovery of novel chemical modulators for members of the therapeutically relevant family of G protein-coupled receptors (GPCRs) is still dominated by ligand-based approaches mainly because of, on one hand, the technical difficulties encountered in crystallizing these receptors and, on the other hand, the large amount of biological data available for molecules acting on these receptors. Accordingly, to illustrate the applicability and performance of SHED for virtual chemical screening on GPCRs, the structures of a set of 24 highly diverse α1A- adrenoceptor antagonists with known binding affinities (Ki < 300 nM) were extracted from a recent publication. The SHED profiles derived from those 24 reference compounds were then used to score a database composed of 3033 drugs and a test set of 15 α1A- adrenoceptor antagonists. The scoring of each compound in the database was simply assigned to the minimum value of all Euclidean distances calculated between the SHED profile of the compound and each one of the 24 reference SHED profiles.

The percentage of actives found with SHED within each percentage of the database is plotted in Figure 4 (black bold line). After rank ordering, selection of the top-ranked 5% and 10% of the compounds in the database would have included 53.3% (8) and 80.0% (12), respectively, of the 15...
\(\alpha_{1A}\)-adrenoceptor antagonists in the test set. In terms of overall enrichment, in the ideal situation that all 15 actives were found in the 15 top-ranked compounds, the value for the normalized area under the curve (AUC) would be 0.9975 (AUC\(_{T}\)), whereas a random identification of actives (symbolized by the thin diagonal line in Figure 4) would result in a normalized AUC of 0.5000 (AUC\(_{0}\)). Correspondingly, the normalized AUC of the resultant active identification line (black bold line) is 0.9220. From these AUC values, an enrichment factor can be defined as \(E = (AUC - AUC_0)/\text{(AUC}_{T} - AUC_0)\). This enrichment factor can have values in the range of \([-1.0, 1.0]\). A value of \(E = -1.0\) would reflect the worst scenario of finding all actives in the database in the last bottom-ranked compounds, whereas a value of \(E = 1.0\) would reflect the ideal situation of finding all actives in the database in the first top-ranked compounds. A random identification of actives would result in \(E = 0.0\). On the basis of this definition, the current virtual screening returns an enrichment of \(E = 0.8482\).

For the sake of comparison, alignment-independent GRIND descriptors derived from three-dimensional molecular interaction fields were also calculated for all compounds using the program ALMOND\(^{25}\) with three-dimensional structures derived by CORINA.\(^{26}\) In this case, the scoring of each compound in the database was assigned to the minimum value of all Euclidean distances calculated between the first five scaled principal component analysis scores of the compound and those corresponding to each one of the 24 reference compounds. The percentage of actives found with GRIND within each percentage of the database is plotted in Figure 4 (gray bold line). After rank ordering, selection of the top-ranked 5\% and 10\% of the compounds in the database would have included 6.7\% (1) and 33.3\% (5), respectively, of the 15 \(\alpha_{1A}\)-adrenoceptor antagonists in the test set. In terms of overall enrichment, the normalized AUC of the resultant active identification line (gray bold line) is 0.7770, which corresponds to an enrichment of \(E = 0.5568\).

The performance of SHED for identifying the test set of 15 \(\alpha_{1A}\)-adrenoceptor antagonists within the top positions of the rank-ordered database may have been masked to some extent by the presence of drugs that might as well have some affinity for the \(\alpha_{1A}\)-adrenoceptor. For instance, droperidol and trazodone were found at ranks 9 and 29, respectively, and were neither in the reference nor in the test set of \(\alpha_{1A}\)-adrenoceptor antagonists. Some examples of drugs that were found within the top ca. 1\% of the rank-ordered database, together with the reference \(\alpha_{1A}\)-adrenoceptor antagonist with the closest SHED profile to that of each drug, are collected in Figure 5. At rank 4, we found WAY 100635, an antagonist of the serotonin 5-HT\(_{1A}\) receptor. The closest \(\alpha_{1A}\)-adrenoceptor antagonist found in the reference set is ARC 239 (p\(K_i = 9.0\)).\(^{24}\) Despite having essentially different scaffolds, the similarities between the structural features of both compounds are remarkable. This result would thus alert one to the possibility of WAY 100635 hitting the \(\alpha_{1A}\)-adrenoceptor as an off target. In fact, evidence can be found in the literature that WAY 100635 induces hypotension in anesthetized rats and that this effect could be partially explained by the antagonism of vascular \(\alpha_{1}\)-adrenoceptors.\(^{27}\) Ketanserin, a serotonin 5-HT\(_2 \) antagonist, was found at rank 14. The closest \(\alpha_{1A}\)-adrenoceptor antagonist found in the reference set is spiperone (p\(K_i = 8.1\)), with which ketanserin shares a similar pharmacological profile on a panel of 75 targets was known.\(^{24}\) The majority of compounds had some affinity for the \(\mu\) opiate receptor, but against a panel of diverse targets,

**Figure 5.** Selection of top-ranked drugs identified in the virtual chemical screening for \(\alpha_{1A}\)-adrenoceptor antagonists. The reference \(\alpha_{1A}\)-adrenoceptor antagonist having the closest SHED profile to each drug is also included. The rank position of the drug is given in parentheses.
they displayed essentially different pharmacological profiles. As illustrative examples, two selected pairs of compounds are shown in Figure 6. Despite the apparent structural differences, compounds 16 and 17 had a similar affinity for the μ opiate receptor, with pIC₅₀ values of 5.98 and 5.83, respectively. However, while the pharmacological profile of compound 16 shows a high selectivity toward the μ opiate receptor, compound 17 has a poor specificity, with a low micromolar affinity for 14 out of 20 GPCR targets. In contrast, compounds 18 and 19 not only had similar high affinities for the μ opiate receptor, with pIC₅₀ values of 7.80 and 7.78, respectively, but showed also comparable overall pharmacological profiles against the panel of 20 GPCRs.

Having the ability to estimate in advance potential deviations in the pharmacological profiles of a list of hits identified in the early stages of a drug discovery project would be of great value to prioritize further optimization activities on those hits. Recent studies have explored the use of similarity metrics to analyze the relationship between the degree of pharmacophore similarity in a pair of compounds and the similarity of their respective pharmacological profiles. The extent to which the SHED profiles introduced in this work reflect the relative pharmacological profiles of compounds is an aspect worth investigating at this stage. To this aim, the SHED profiles for the two pairs of compounds described above have been included also in Figure 6. A comparison of the SHED profiles obtained for compounds 16 and 17 evidences dissimilar feature distributions, the profile for compound 17 covering clearly a wider SHED area consistent with the larger size of this molecule relative to that of 16. In contrast, compounds 18 and 19 showed visibly similar SHED profiles, consistent with a pair of compounds of approximately the same size containing similar features arranged similarly.

At a more quantitative level, as proposed in a previous study, an activity dissimilarity score of the pharmacological profiles of two compounds can be defined as

\[ D(A,B) = \sum \Delta[\text{inh}(A) - \text{inh}(B)] \]

where %inh stand for the percentages of inhibition (at 10 μM) of A and B in the test i among 75 tests of the profile. The term

\[ \Delta[\text{inh}(A) - \text{inh}(B)] \]

was originally defined as an empirical measure of how different the two compounds behave with respect to that test:

\[ \Delta(x) = \begin{cases} 0 & \text{if } x \leq 30 \\ (x - 30)/40 & \text{if } 30 < x \leq 70 \\ 1 & \text{if } x > 70 \end{cases} \]

As an example, Figure 6 contains also the values obtained for the dissimilarity of pharmacological profiles and SHED profiles between the two illustrative pairs of compounds. The visual observation that the pharmacological profiles of compounds 16 and 17 differ much more than those of compounds 18 and 19 is reflected in dissimilarity values of 24.7 and 2.6, respectively. Correspondingly, the differences observed in the SHED profiles of compounds 16 and 17 compared to those of compounds 18 and 19 result in dissimilarity values of 5.2 and 1.0, respectively. These results are illustrative of the potential use of SHED profiles as a means for alerting one to likely differences or similarities in the pharmacological profiles of series of molecules for which experimental affinities are available only for a particular target.

To investigate this issue further, SHED and pharmacological profile dissimilarities were evaluated for each of the pairwise combinations of the 47 compounds, in an analogous way to that reported in the previous study from which the
structures and experimental binding affinities of compounds were extracted. Then, all pairs of compounds were sorted into dissimilarity categories. The resultant distribution of the pairs in each category versus the dissimilarity scores obtained for the calculated SHED profiles and the observed pharmacological profiles is given in Figure 7. For each pair of compounds, the dissimilarity of SHED profiles refers to the Euclidean distance between their SHED profiles, whereas the dissimilarity of pharmacological profiles accounts for the differences in their respective percentages of inhibition accumulated over the entire set of biologically relevant targets to which the compounds were tested against, as detailed above. Remarkably, the overall distribution presented in Figure 7 reproduces qualitatively the results obtained in the earlier parent study (see Figure 2 in ref 31). In the class of compounds having the most similar feature distributions (dissimilarity of SHED profiles ≤ 2), the occurrence of pharmacologically similar compound pairs (dissimilarity of pharmacological profiles ≤ 5) is significantly high. With an increasing dissimilarity of SHED profiles, the relative probability of finding pairs of compounds with similar pharmacological profiles decreases considerably. Consequently, pairs of compounds having similar SHED profiles are more likely to have similar pharmacological profiles than any random pair of dissimilar molecules.

**CONCLUSIONS**

We have introduced SHED as a novel set of molecular descriptors based on the information-theoretical concept of Shannon entropy applied to quantifying the variability displayed by topological distributions of atom-centered feature pairs in chemical structures. Under this new representation, molecules containing comparable features arranged similarly around essentially different scaffolds give rise to similar SHED profiles, illustrated in this work for the cases of cyclooxygenase-1 inhibitors, thrombin inhibitors, and estrogen α antagonists. This property was then further assessed in a virtual chemical screening exercise to retrieve 15 α1A-adrenoceptor antagonists from a database of 3033 drugs. Using a reference set of 24 diverse α1A-adrenoceptor antagonists, selecting the top-ranked 10% of the compounds in the database would have included 80.0% of the α1A-adrenoceptor antagonists in the test set, with an overall enrichment factor of 0.8482. In addition, the use of SHED helped to identify the α1A-adrenoceptor as a potential off target for several top-ranked drugs. Finally, SHED profiles demonstrated a decent performance for estimating differences in the virtual pharmacological profiling of molecules, with pairs of compounds having similar SHED profiles showing a trend toward also having similar pharmacological profiles.

Given the large amount of experimental data available currently on the affinity of molecules to targets, ligand-based approaches to drug discovery remain still competitive against more sophisticated structure-based methods. In view of the results presented here, the use of SHED appears as a simple, yet attractive, low-dimensional representation of molecules with promising applicability for the virtual identification and profiling of novel hits at the early stages of drug discovery projects.

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**Supporting Information Available:** The mapping of Sybyl atom types to pharmacophoric features; feature-pair distributions and the SHED profile for dimetindene; SHED profiles for COX-1, thrombin, and estrogen ligands; and the structures of the 39 α1A-adrenoceptor antagonists used in the virtual chemical screening. This material is available free of charge via the Internet at http://pubs.acs.org.

**REFERENCES AND NOTES**


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